



Dynamics & Coupling

2007-2008 progress report

Filip Váňa

`filip.vana@chmi.cz`

CHMI



New interpolators for SL



Work of: **J. Mašek (Sk)** and **F. Váňa (Cz)**

- The Lagrangian cubic interpolation is replaced by a general two-parametric interpolator:

$$F(x, \mathbf{y}) = w_0(x)y_0 + w_1(x)y_1 + w_1(1-x)y_2 + w_0(1-x)y_3$$

where $\mathbf{y} = (y_0, y_1, y_2, y_3)$

$$w_0(x) = a_1x + a_2x^2 - (a_1 + a_2)x^3$$

$$w_1(x) = 1 + (a_2 - 1)x - (3a_1 + 4a_2)x^2 + 3(a_1 + a_2)x^3$$



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- Any interpolator F in (a_1, a_2) plane can be composed as a linear combination of (three) other interpolators:

$$F = \kappa_1 F_1 + \kappa_2 F_2 + (1 - \kappa_1 - \kappa_2) F_3$$



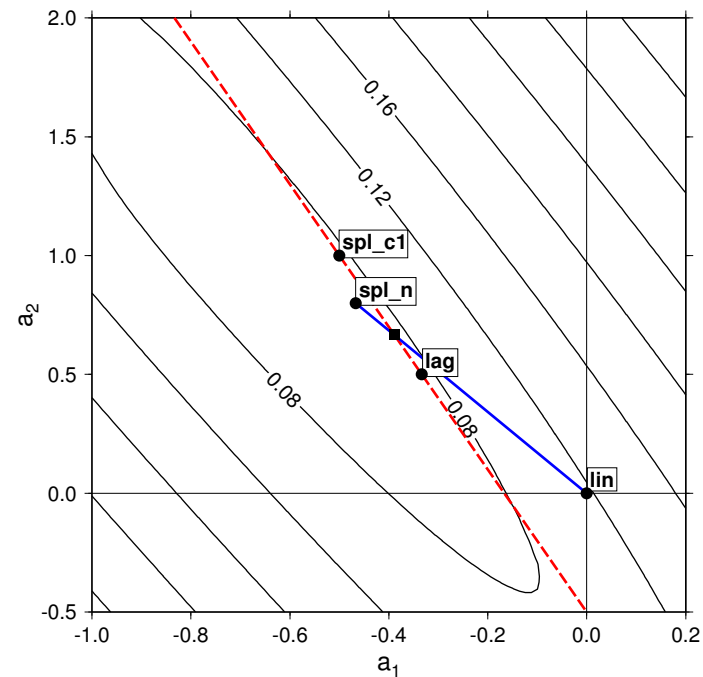
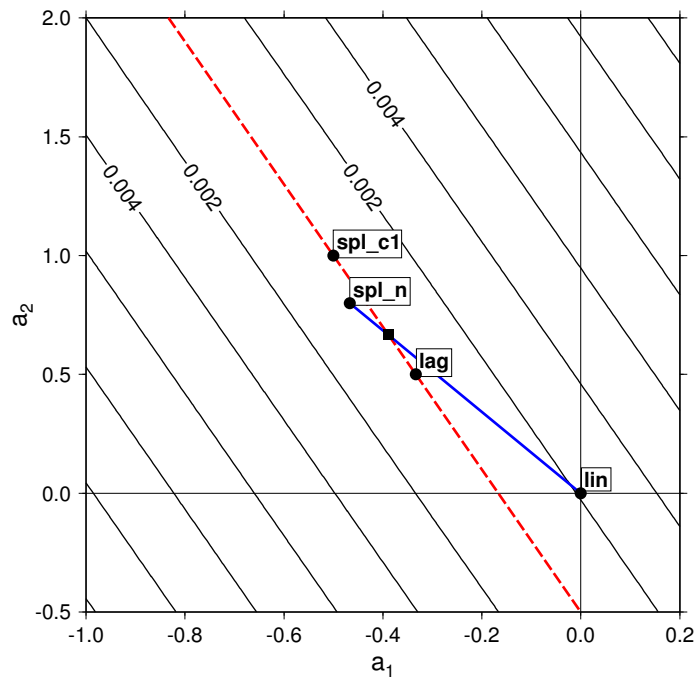


New interpolators for SL

Mean absolute error of interpolation

Mean absolute error of interpolators, $w = \exp(-25.m/M)$

Mean absolute error of interpolators, $w = \exp(-m/M)$



GMT 2007 Apr 20 08:46:18



GMT 2007 Apr 20 08:46:13

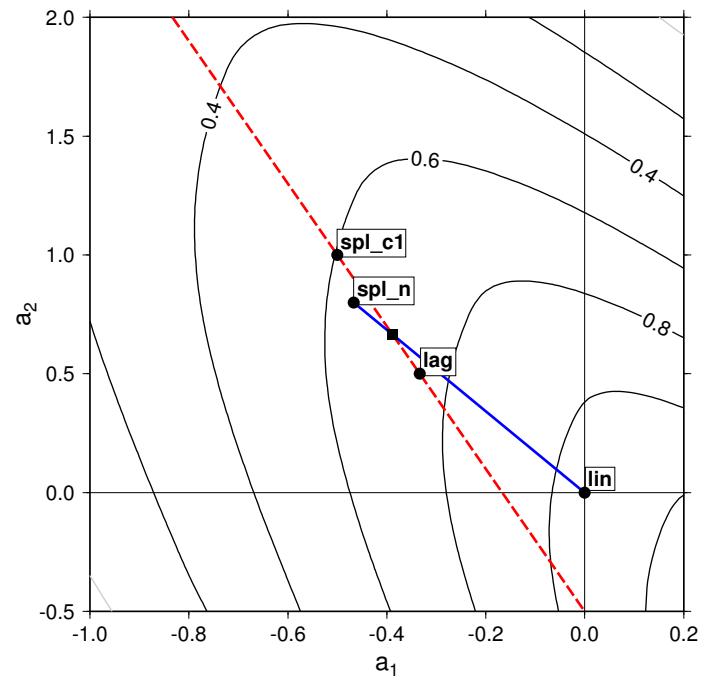
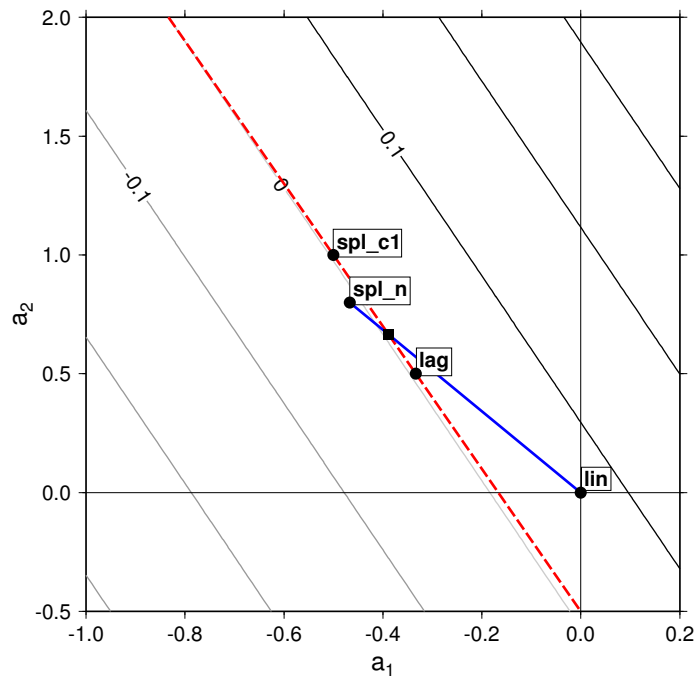


New interpolators for SL

Dimensionless damping rate

Damping factor for $N = 100, m = 10$

Damping factor for $N = 100, m = 40$



GMT 2007 Apr 20 08:45:58



GMT 2007 Apr 20 08:43:48

New interpolators for SL



Implementation guidelines

- The implemented scheme allows at least 2^{nd} order accuracy (given by $6a_1 + 2a_2 = -1$), leaving just one tunable parameter to control the interpolation property.



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- The new data-flow (including the TL/AD code) is available from CY35T1.



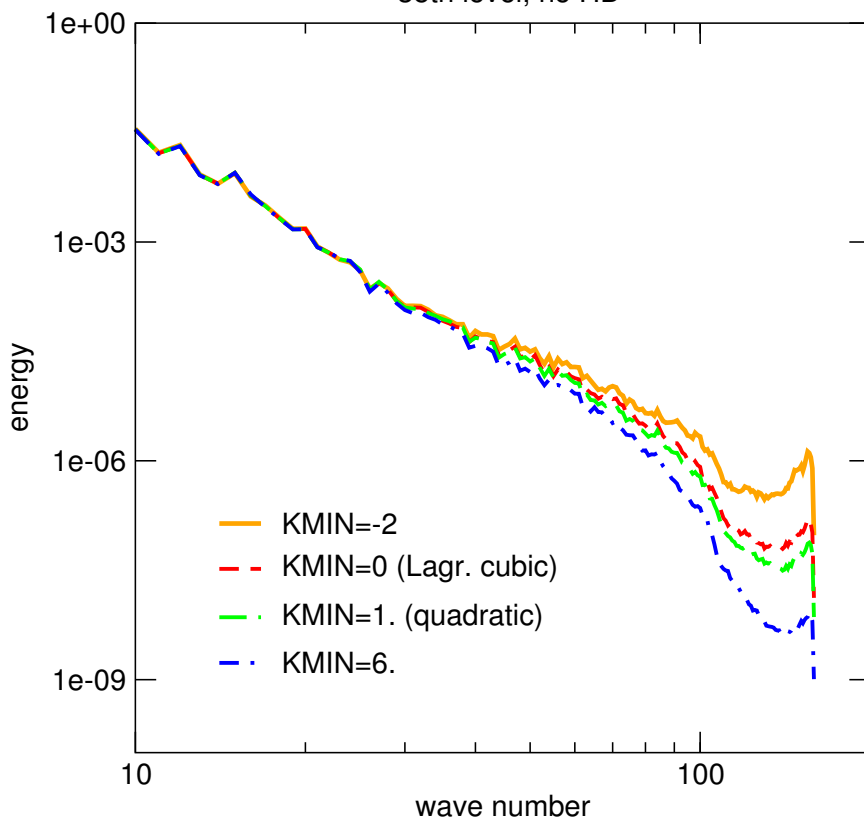


New interpolators for SL

3h adiabatic forecast

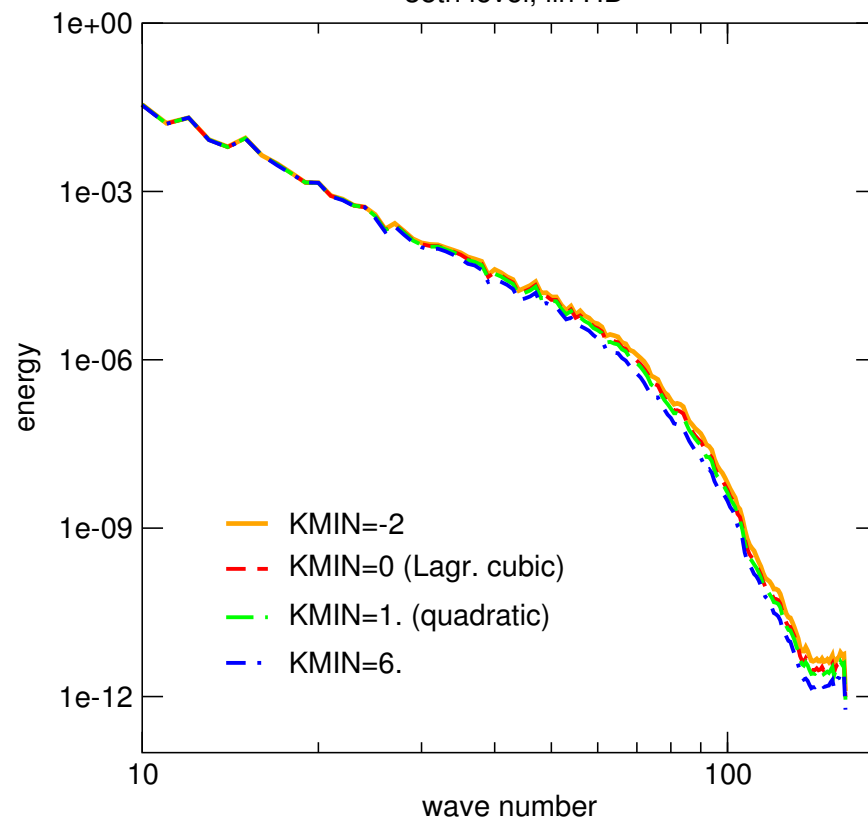
kinetic energy spectra

35th level, no HD



kinetic energy spectra

35th level, lin HD



New features in SLHD



Work of: **J. Mašek (Sk)**, **F. Váňa (Cz)** and **P. Bénard (Fr)**

- SLHD becomes just a special case of the general interpolator F :

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- In agreement with the common practice of the expression of the sub-grid scale lateral diffusion, the physically negligible isotropic term is favorized to prevent spurious accumulation of inertia-gravity wave energy near the cut-off wavenumber. $\Rightarrow \kappa = \kappa(d, \text{DIV})$



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- The triggering function κ can be optionally computed along true p -surfaces (using chain rule to evaluate horizontal derivatives) in order to prevent spurious circulation above sloped terrain.



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- The triggering function κ can be optionally computed along true p -surfaces (using chain rule to evaluate horizontal derivatives) in order to prevent spurious circulation above sloped terrain.
- Optionally the 3D grid-point laplacian is available as the damping operator.

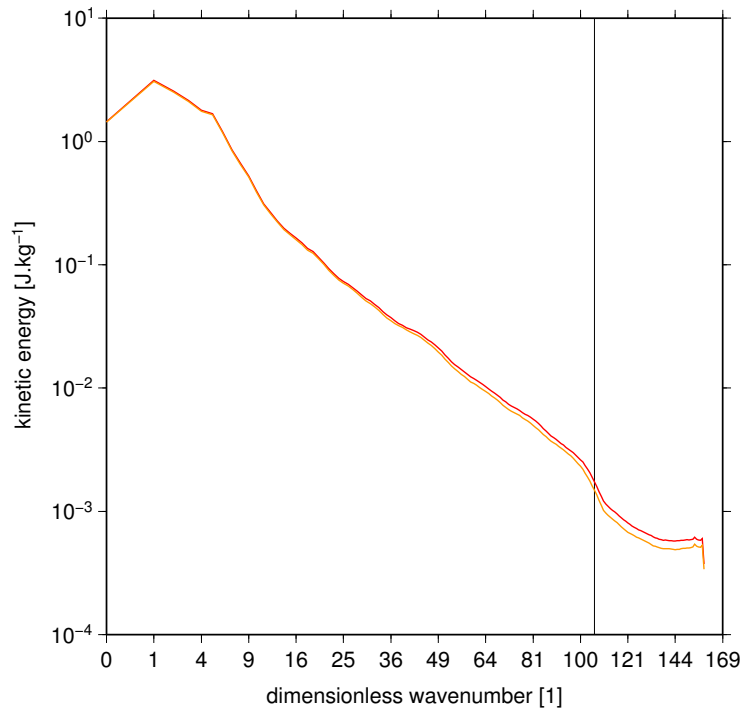




New features in SLHD

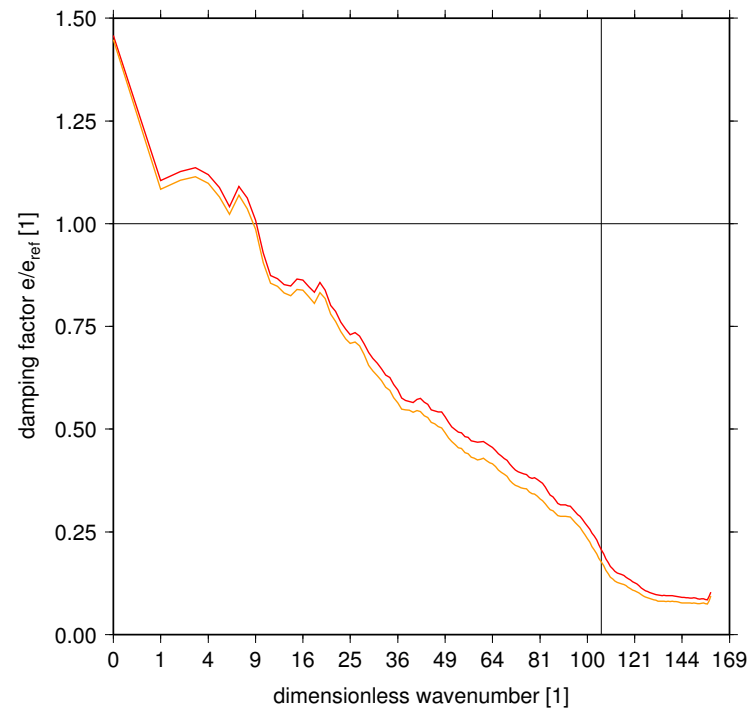
Impact of horizontal triggering, Alps $\Delta x=2.5$ km

Kinetic energy spectrum
(+0006 hour forecast, model level 041)



— deformation computed along η -surfaces
— deformation computed along p -surfaces

Spectral damping by SLHD scheme
(+0006 hour forecast, model level 041)



— deformation computed along η -surfaces
— deformation computed along p -surfaces



2008 Oct 1 11:57:35 K033.K043



2008 Oct 1 11:54:49 K033.K043

New features in SLHD



Laplacian transformed to weights

Applying 2nd order diffusion to interpolated quantity y :

$$\begin{aligned}\tilde{y} &= (1 + \varepsilon \Delta x^2 \partial_x^2) y \\ &= (1 + \varepsilon \Delta x^2 \partial_x^2) w_1 (y_1 - y_0) + w_2 (y_2 - y_0) + w_3 (y_3 - y_0)\end{aligned}$$





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The diffusion operator can be transformed into weights:

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$$\text{with } \begin{pmatrix} \tilde{w}_1 \\ \tilde{w}_2 \\ \tilde{w}_3 \end{pmatrix} = \begin{pmatrix} 1 - 2\varepsilon & \varepsilon & 0 \\ \varepsilon & 1 - 2\varepsilon & 0 \\ 0 & \varepsilon & 1 \end{pmatrix} \cdot \begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix}$$



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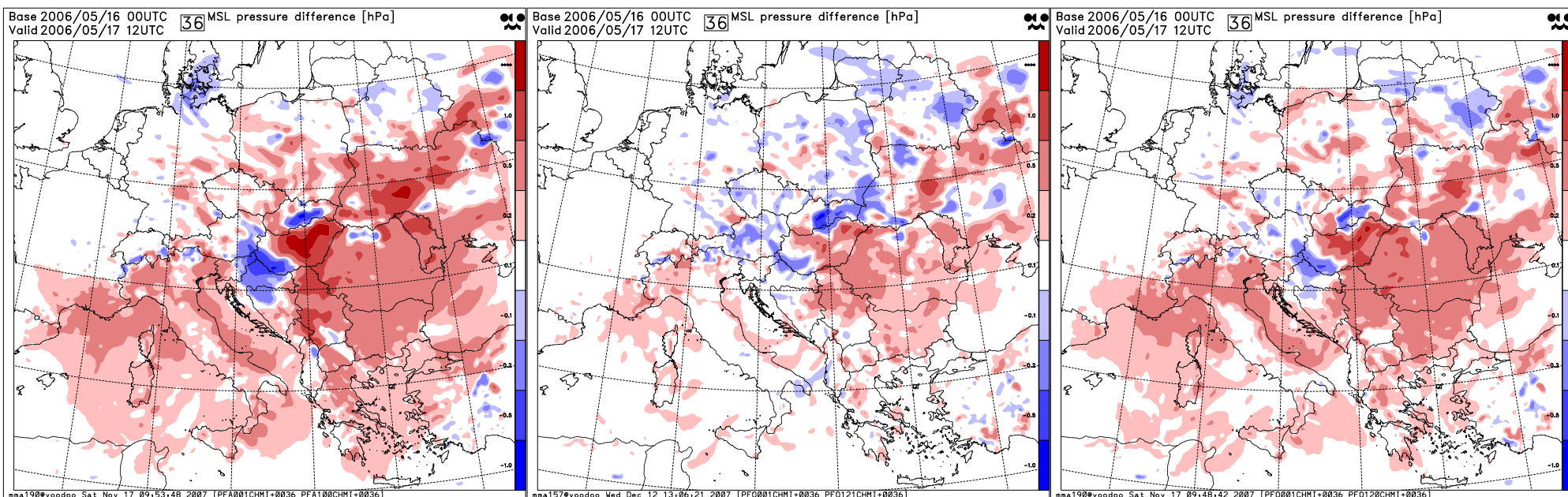
The implementation distinguish between ε_H and ε_V





New features in SLHD

Impact of SLHD to MSL pressure bias



old SLHD

new SLHD

new SLHD; $\epsilon_V = 0.02$

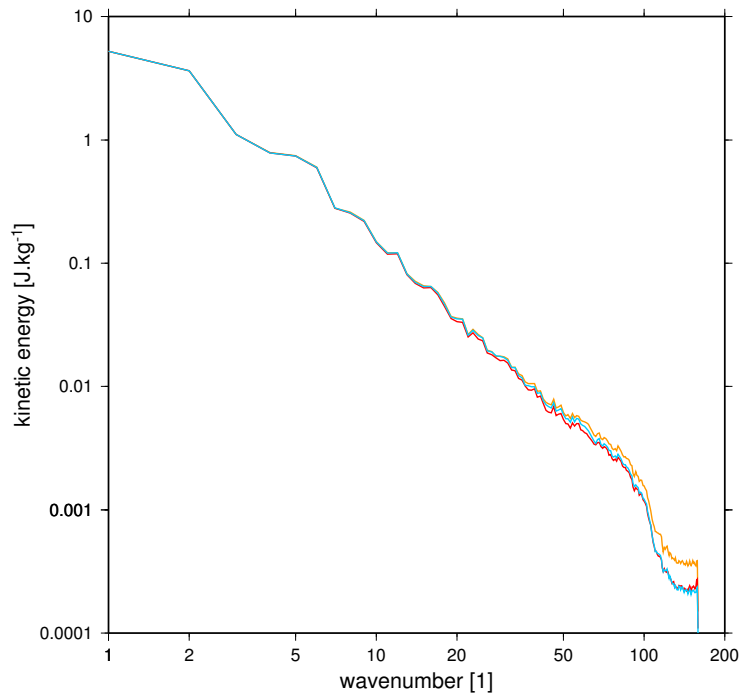




New features in SLHD

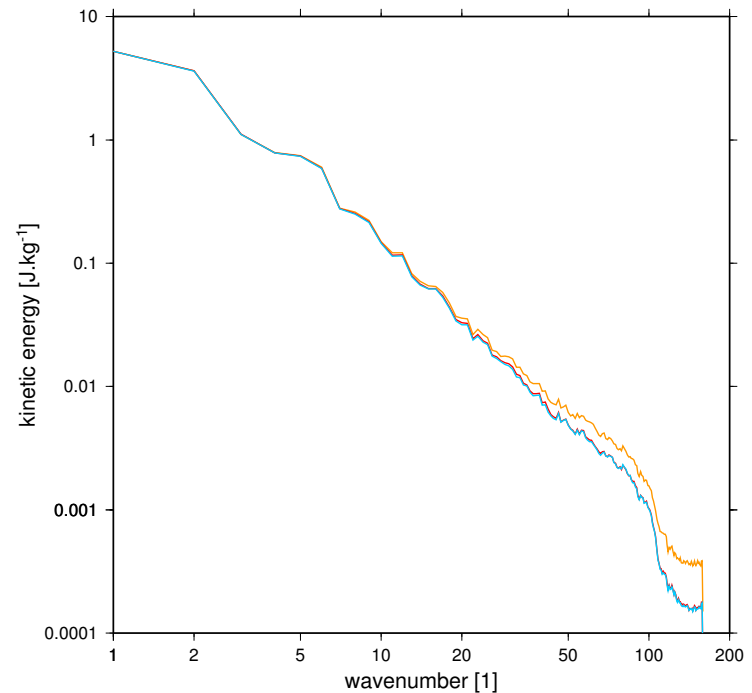
Impact to KE spectra

Impact of gridpoint part of SLHD
(kinetic energy spectra, level 041, t = +0006 h)



- gridpoint part of SLHD, lag
- gridpoint part of SLHD, $(1-\kappa).lag + \kappa.quad$ ($-2 < \kappa < 6$), $\epsilon_H = 0.02$
- gridpoint part of SLHD, $(1-\kappa).lag + \kappa.quad$ ($0 < \kappa < 6$), $\epsilon_H = 0$

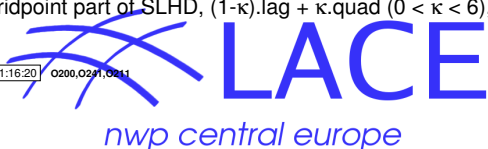
Impact of gridpoint part of SLHD
(kinetic energy spectra, level 041, t = +0006 h)



- gridpoint part of SLHD, lag
- gridpoint part of SLHD, lag_s, $\epsilon_H = 0.05$, $\epsilon_V = 0$
- gridpoint part of SLHD, lag_s, $\epsilon_H = 0.05$, $\epsilon_V = 0.05$



GMT 2007 Dec 13 11:16:20 0200,0230,0231



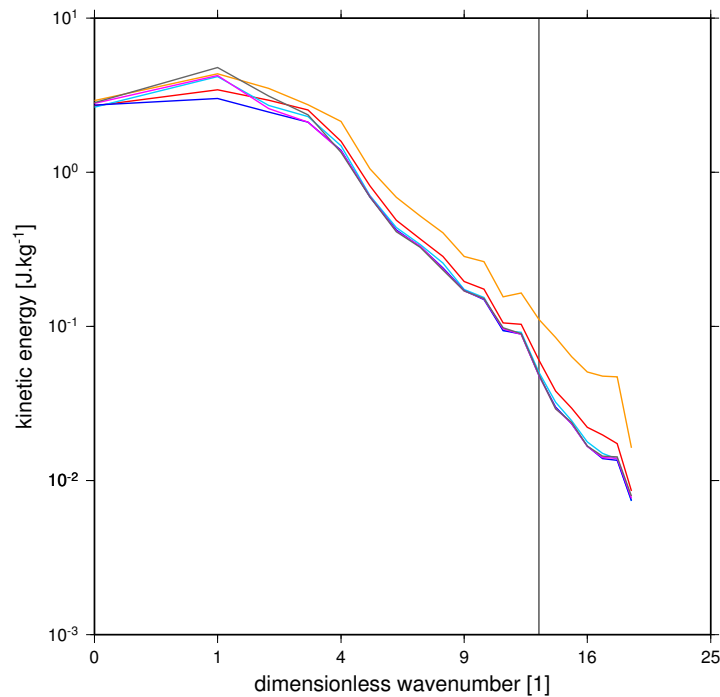
GMT 2007 Dec 12 13:55:08 0200,0230,0231



New features in SLHD

Impact of Δt

Kinetic energy spectrum
(+0006 hour forecast, model level 041)



- dt = 1440s
- dt = 720s
- dt = 360s
- dt = 180s
- dt = 90s
- dt = 45s



GMT 2008 Jun 9 09:25:30 K900,K901,K902,K903,K904,K905

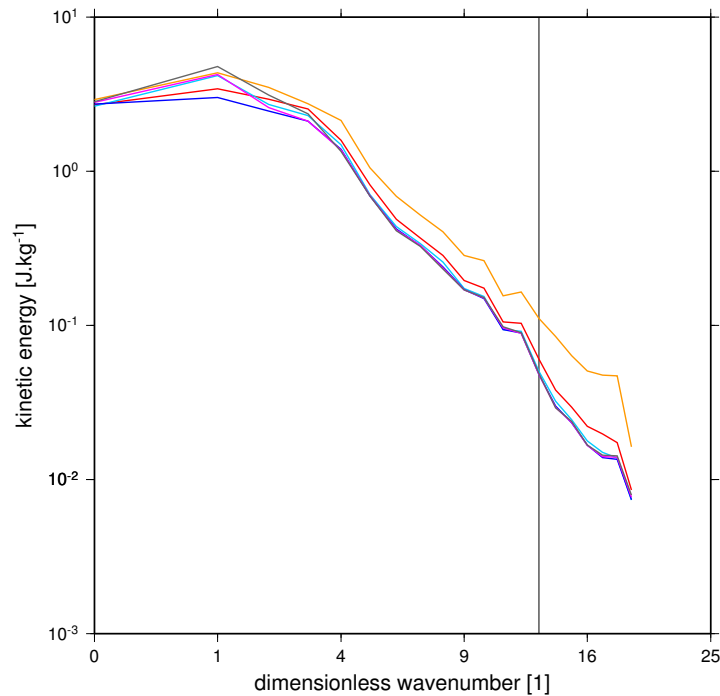




New features in SLHD

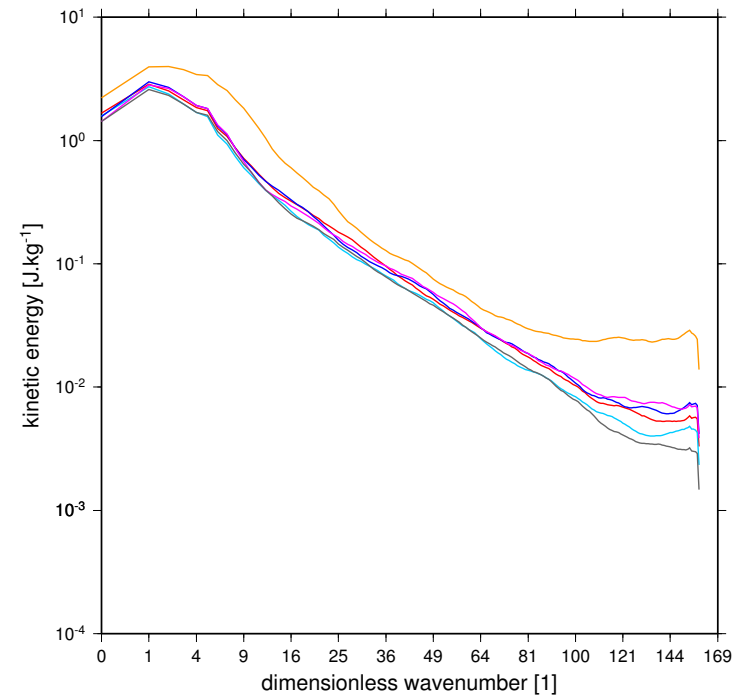
Impact of Δt

Kinetic energy spectrum
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- dt = 1440s
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Sensitivity of kinetic energy spectrum to SLHDA0
(+0006h forecast, model level 041, dx = 2.5km, lag + quad, NITMP = 2)



- SLHDA0 = 24.8
- SLHDA0 = 24.9
- SLHDA0 = 25.0
- SLHDA0 = 25.1
- SLHDA0 = 25.2
- SLHDA0 = 25.3



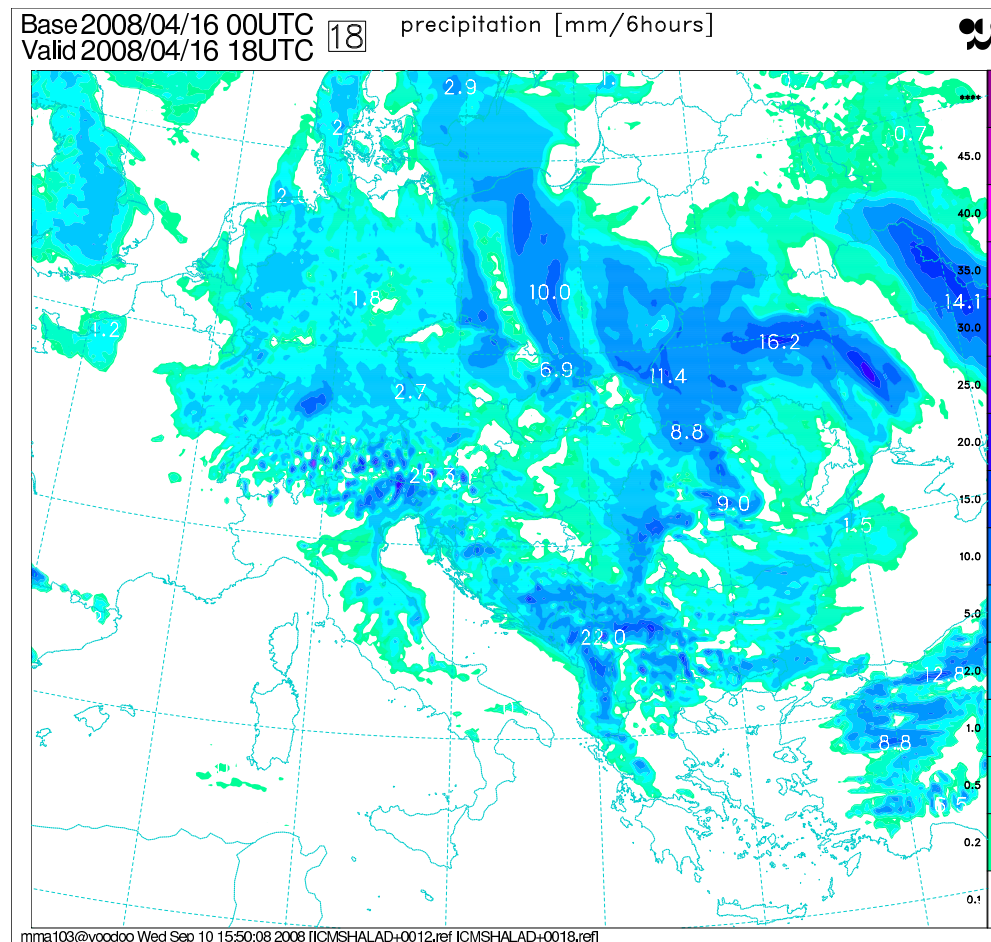
GMT 2008 Jun 9 09:25:30 K900,K901,K902,K903,K904,K905



GMT 2008 Jun 13 07:22:34 L608,L609,L600,L601,L602,L603

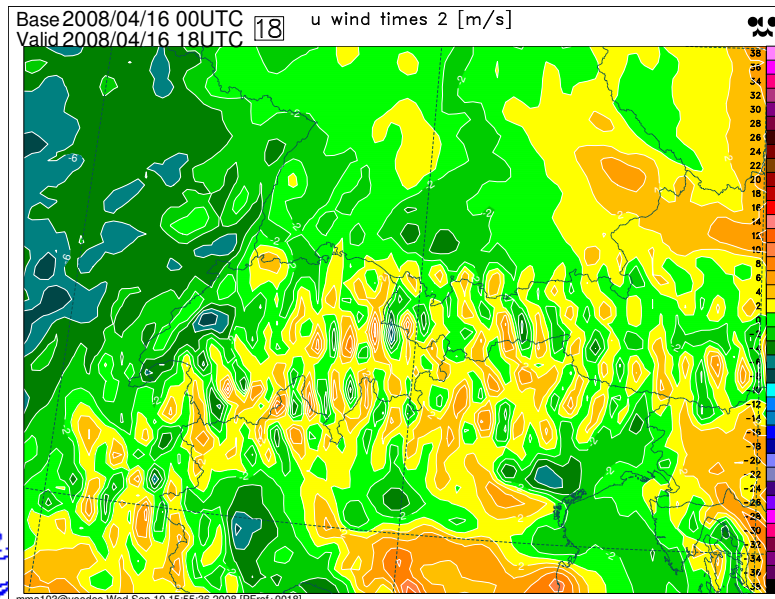
Spectral orography representation

Work of: **F. Váňa and R. Brožková (Cz)**



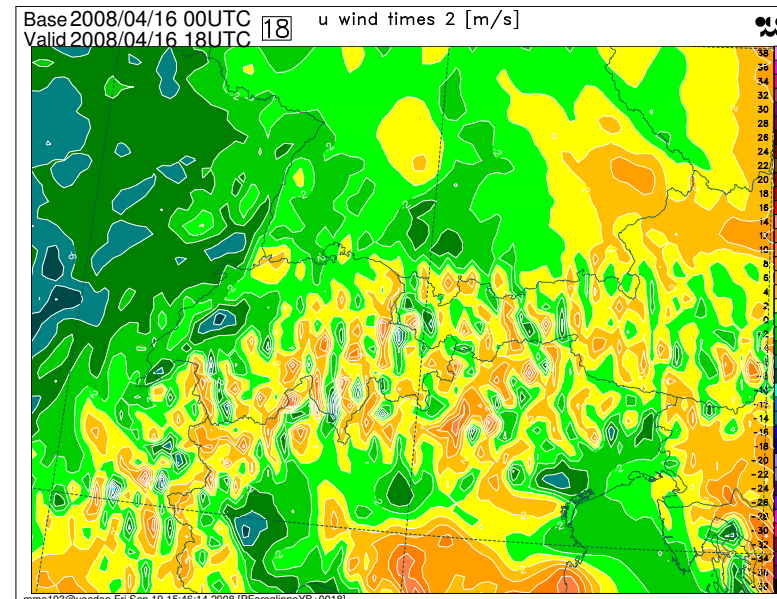
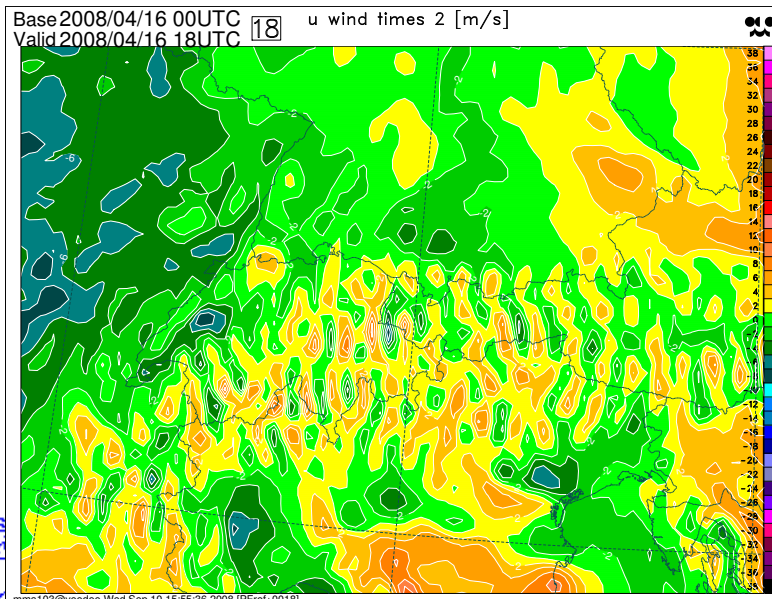
Spectral orography representation

- Quadratic orography modified according Bouteloup (MWR, 1995)



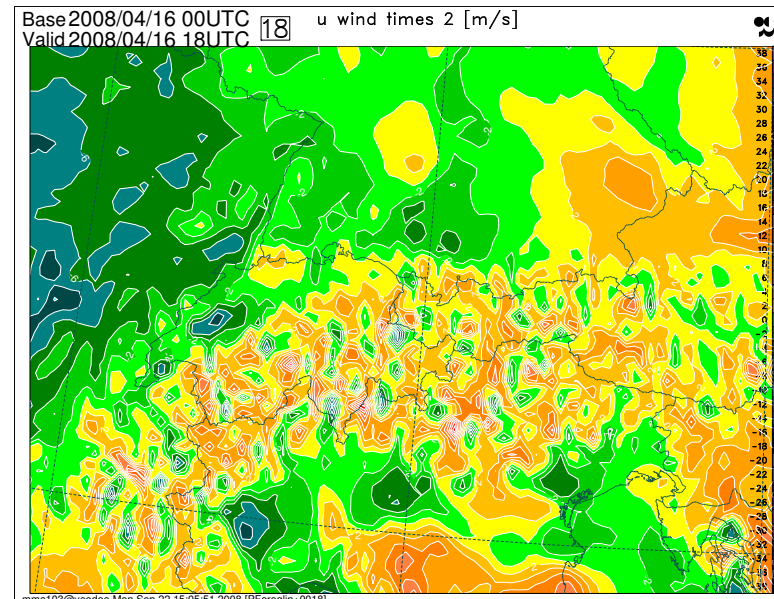
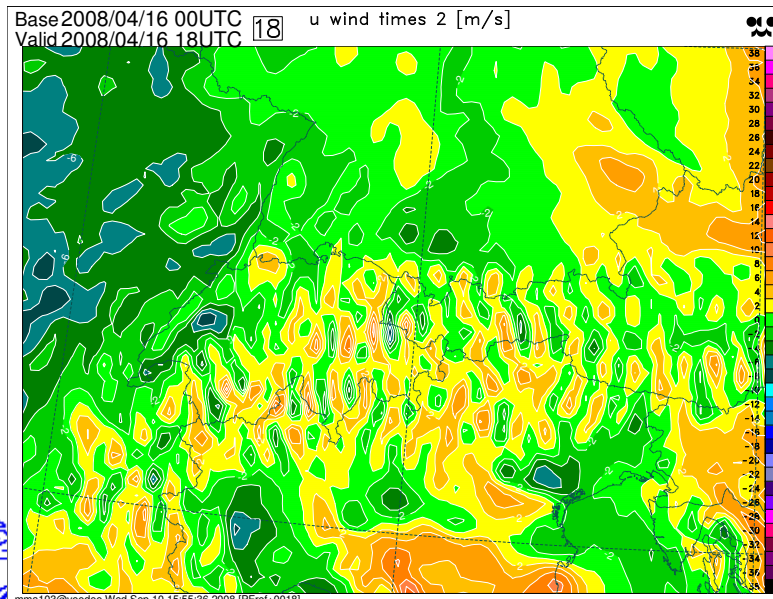
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- Linear orography filtered by diffusion operator



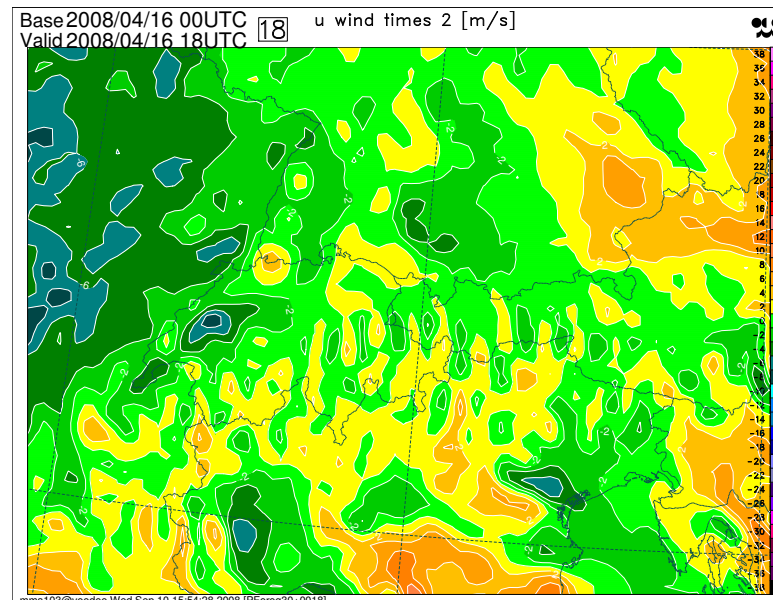
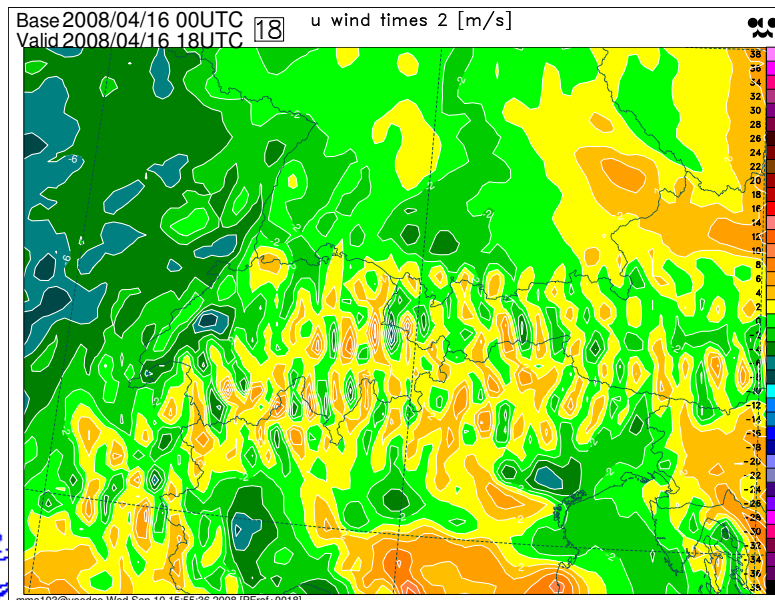
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- Linear orography filtered by diffusion operator
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- Quadratic orography, no filtering

⇒ A new cost function formulation ought to be defined. The E-zone seems to be an attractive place to displace the "noise" from model flat areas.



Other topics



- Implementation of the fully compressible flux conservative thermodynamic equations
Work of: **P. Smolíková and R. Brožková (Cz)**



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Work of: **P. Smolíková and R. Brožková (Cz)**
- Interaction of DFI with the way how the derivatives of RT are computed
Work of: **P. Smolíková and R. Brožková (Cz)**



Other topics



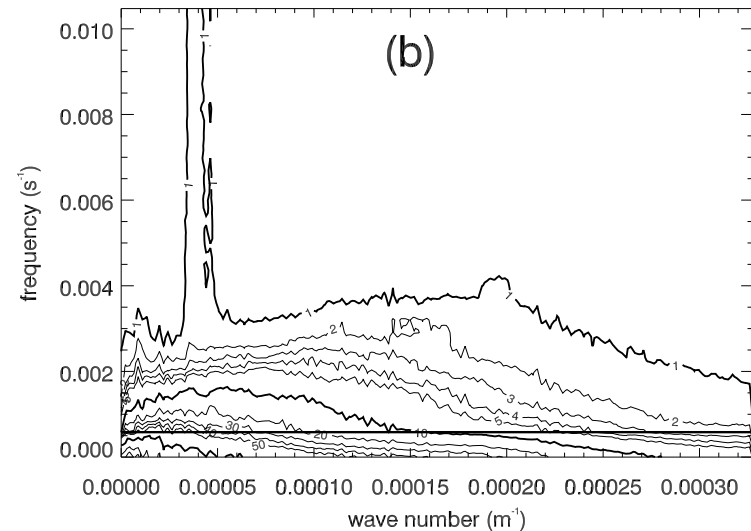
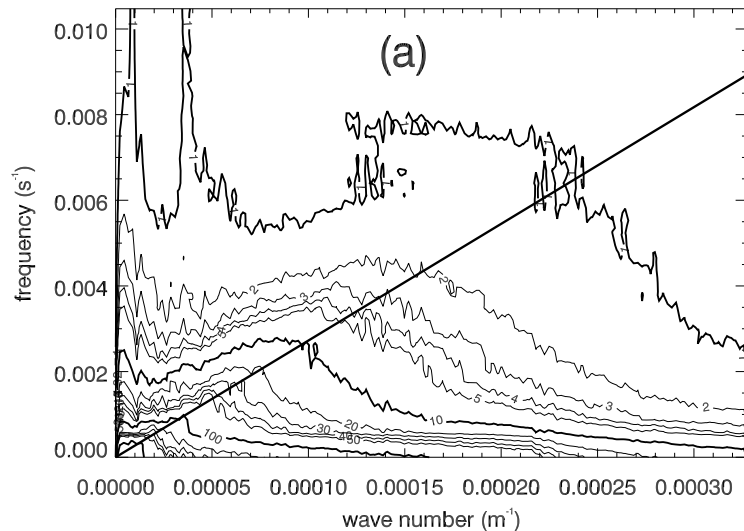
- Implementation of the fully compressible flux conservative thermodynamic equations
Work of: **P. Smolíková and R. Brožková (Cz)**
- Interaction of DFI with the way how the derivatives of RT are computed
Work of: **P. Smolíková and R. Brožková (Cz)**
- 2^{nd} order accurate physics-dynamics interface
Work of: **I. Bašták-Durán (Sk), P. Termonia and R. Hamdi (Be)**



Scale selective DFI



Spectrum in time and space



The Lothar storm $\ln p_s$ decomposed between 0600 UTC and 1200 UTC on 28 December 1999. The thick line is the propagation speed of the storm in this time interval: 98 km/h.

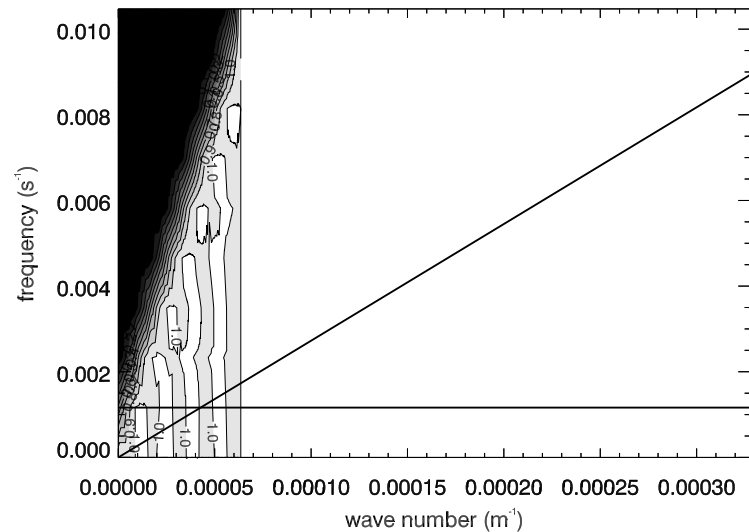
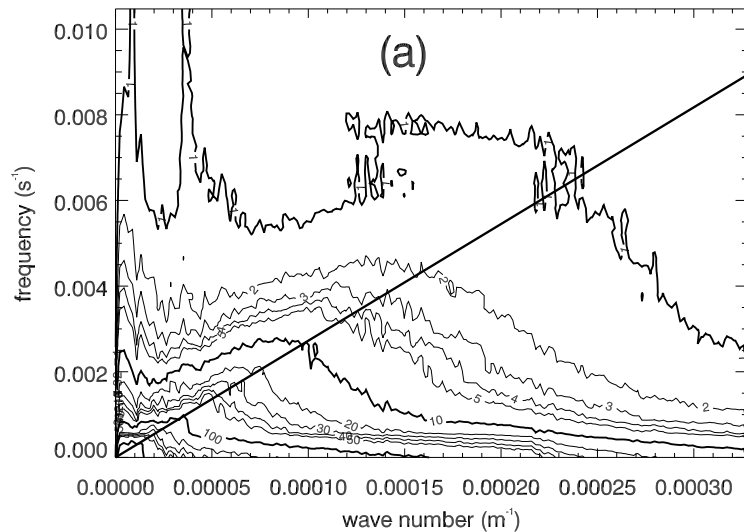
$\ln p_s$ decomposed between 0600 UTC and 1200 UTC of an anticyclonic case on 28 December 1999. The thick horizontal line corresponds to a filter cut-off period of 3 h.



Scale selective DFI



Scale-selective low-pass windows



The *scale-selective* cut-off frequency of a low-pass Lancsoz filter:

$$\omega_c(\kappa) = \begin{cases} \omega_c^0 + \frac{\kappa}{\kappa_c} \left(\frac{\pi}{\Delta t} - \omega_c^0 \right) & \text{if } \kappa \leq \kappa_c \\ \frac{\pi}{\Delta t} & \text{if } \kappa > \kappa_c \end{cases}$$

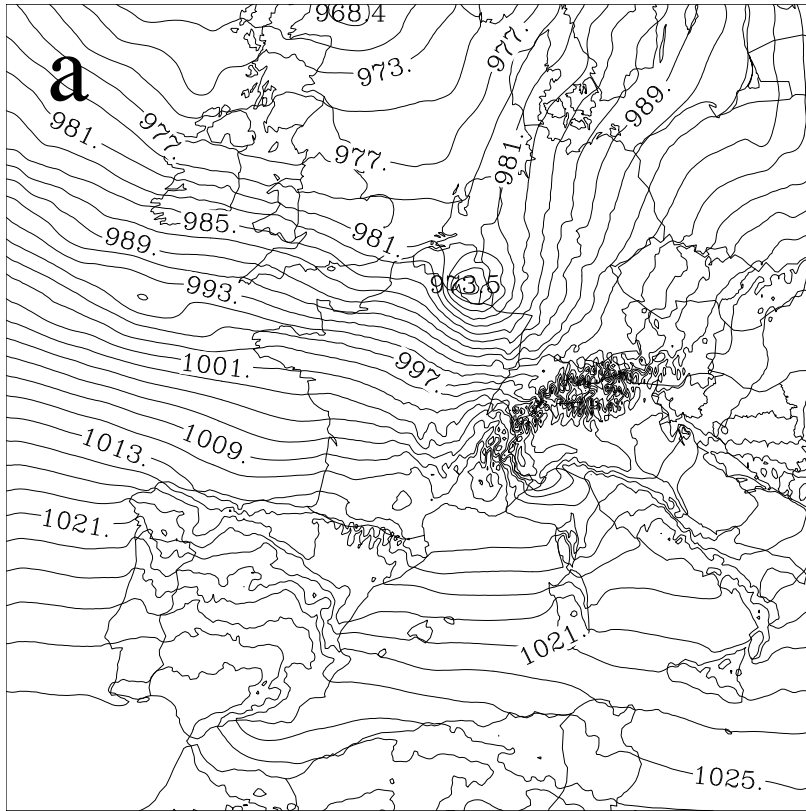
The cut-off period is $T_c^0 = 2\pi/\omega_c^0$ while the *slope* of the cut-off frequencies is $c = \pi/(\kappa_c \Delta t)$.



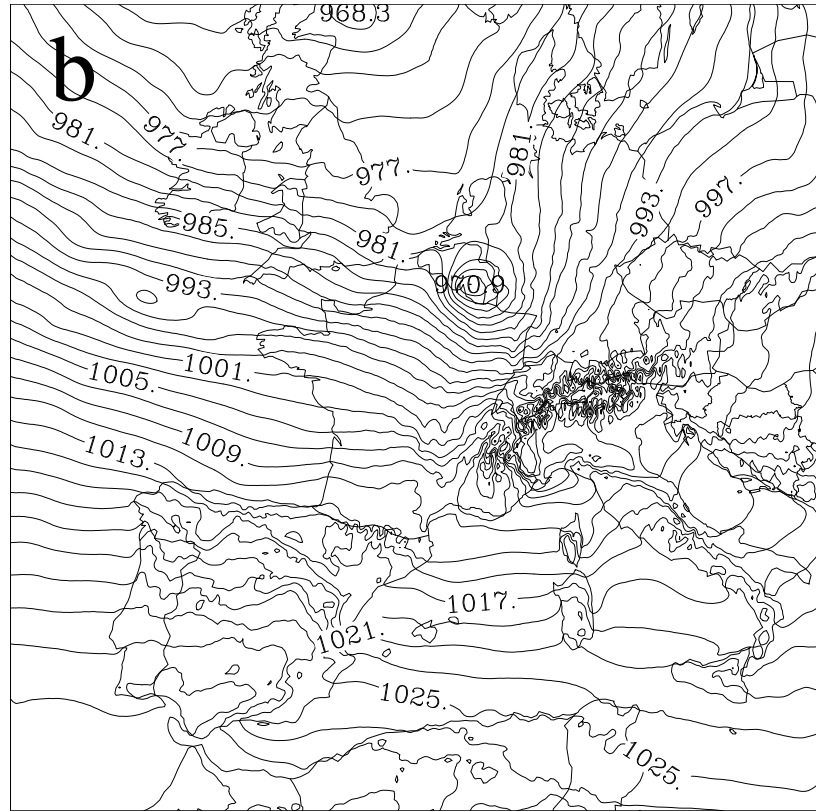
Scale selective DFI



Results:



a run with $T_c^0 = 3h$ (**973.5 hPa**).



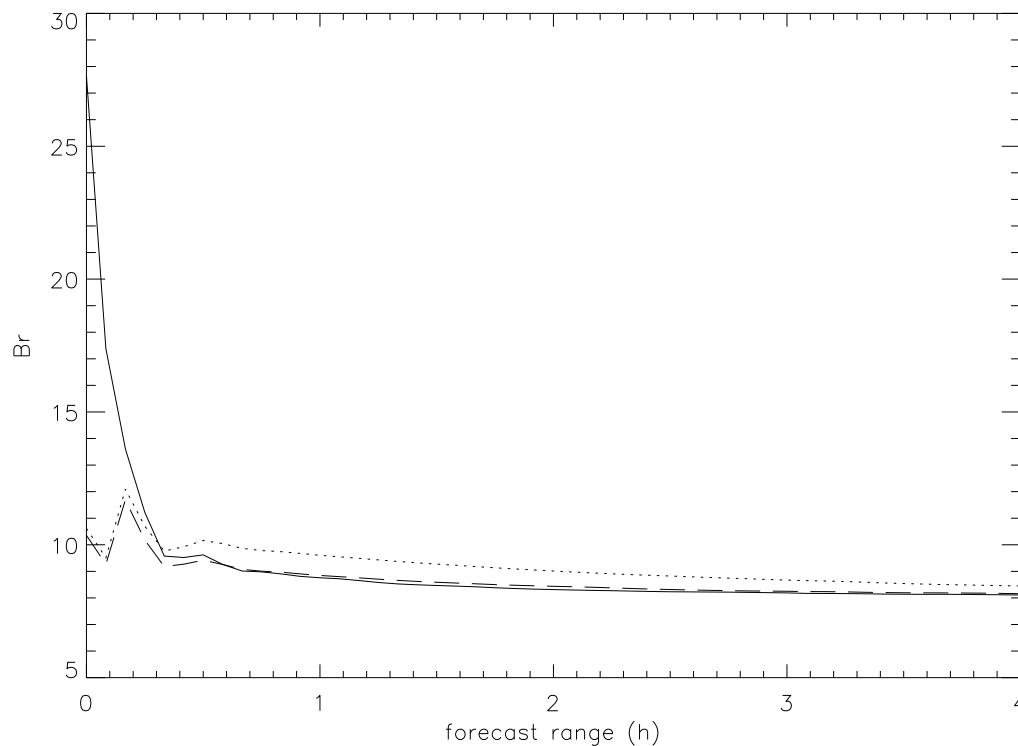
a run with $T_c^0 = 1.5h$ (**970.9 hPa**).



Scale selective DFI



$$Br = 100 \frac{\sum_{IJ} |\sum_L \nabla \cdot \Delta p_L \mathbf{V}_{IJL}|}{\sum_{IJ} \sum_L |\nabla \cdot \Delta p_L \mathbf{V}_{IJL}|} \quad (\text{Lynch and Huang, MWR, 1992})$$



solid: uninitialized

dots: full DFI

dashed: SSDFI_{1.5h}

There are 2 surprises:

- filtering *less*
(SSDFI_{1.5h}) ⇒ *more*
balanced!
- but, full DFI is *worse*
than uninitialized after
half and hour!?

DFI actually creates an unbalance in the *slow* part of the part of dynamics! So it needs a longer time to adjust.

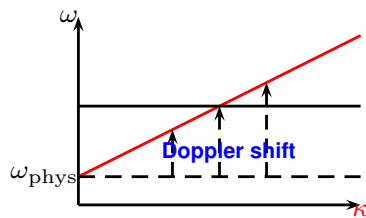




Scale selective DFI

Going to higher resolution

$\Delta x = 10 \text{ km} \rightarrow \Delta x = 2 \text{ km}$: problems smaller with ($5\times$) propagation speeds:



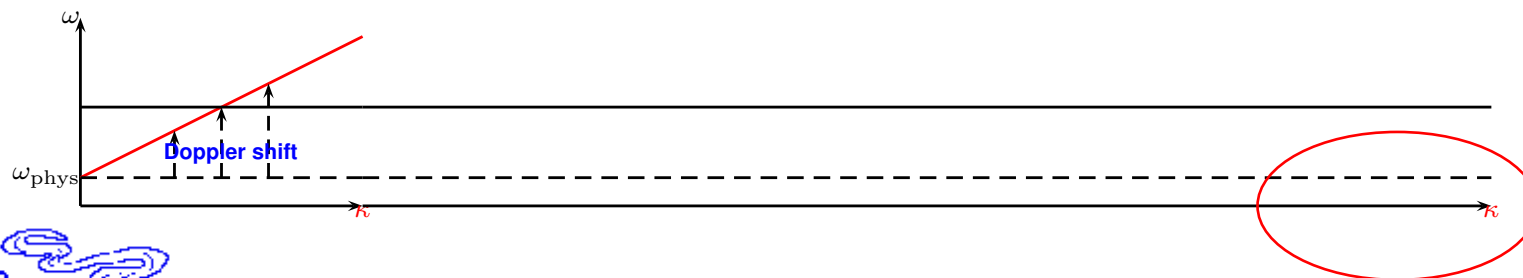


Scale selective DFI

Going to higher resolution

$\Delta x = 10 \text{ km} \rightarrow \Delta x = 2 \text{ km}$: problems smaller with (5 \times) propagation speeds:

$$\omega = \omega_{\text{phys}} + c\kappa$$



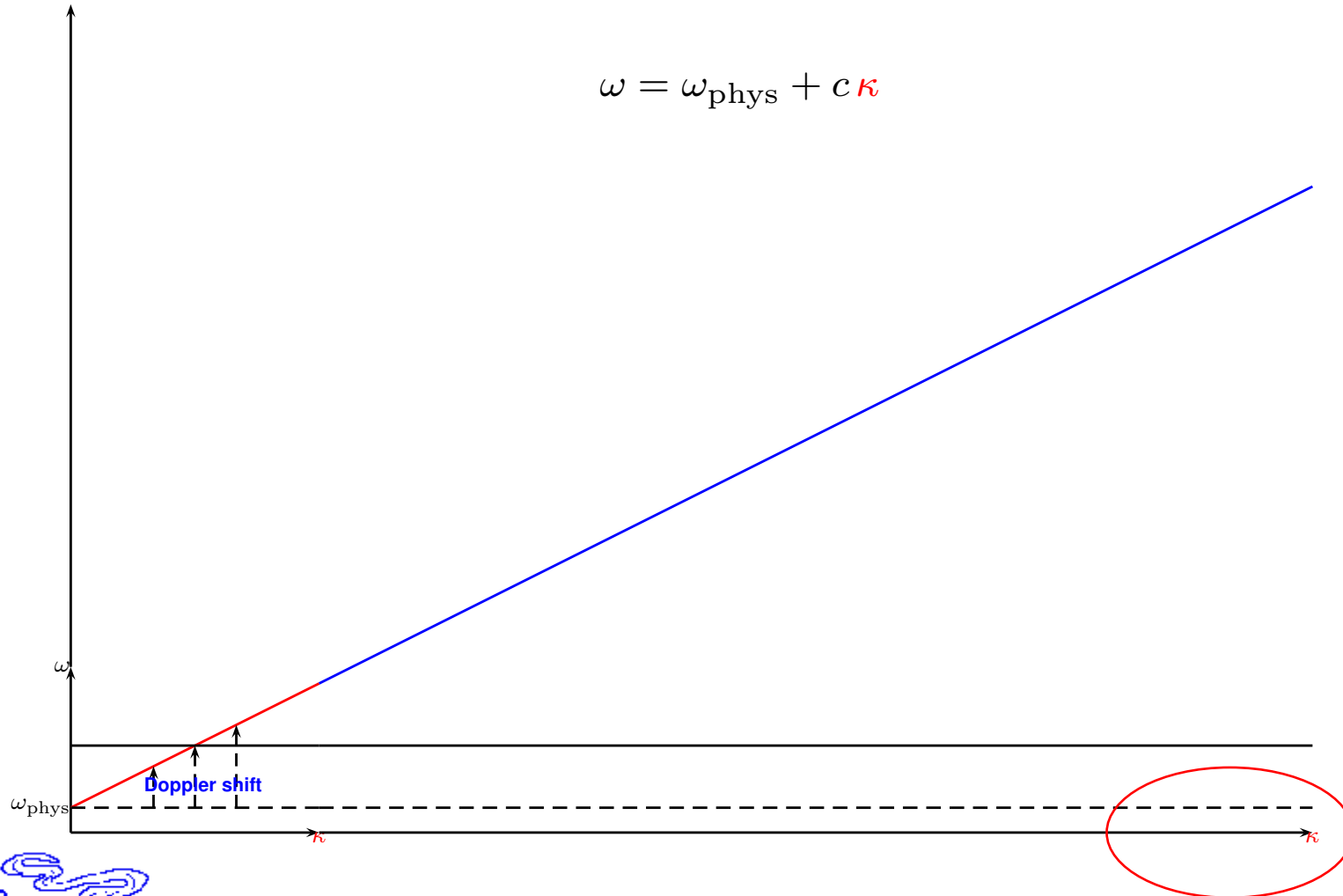


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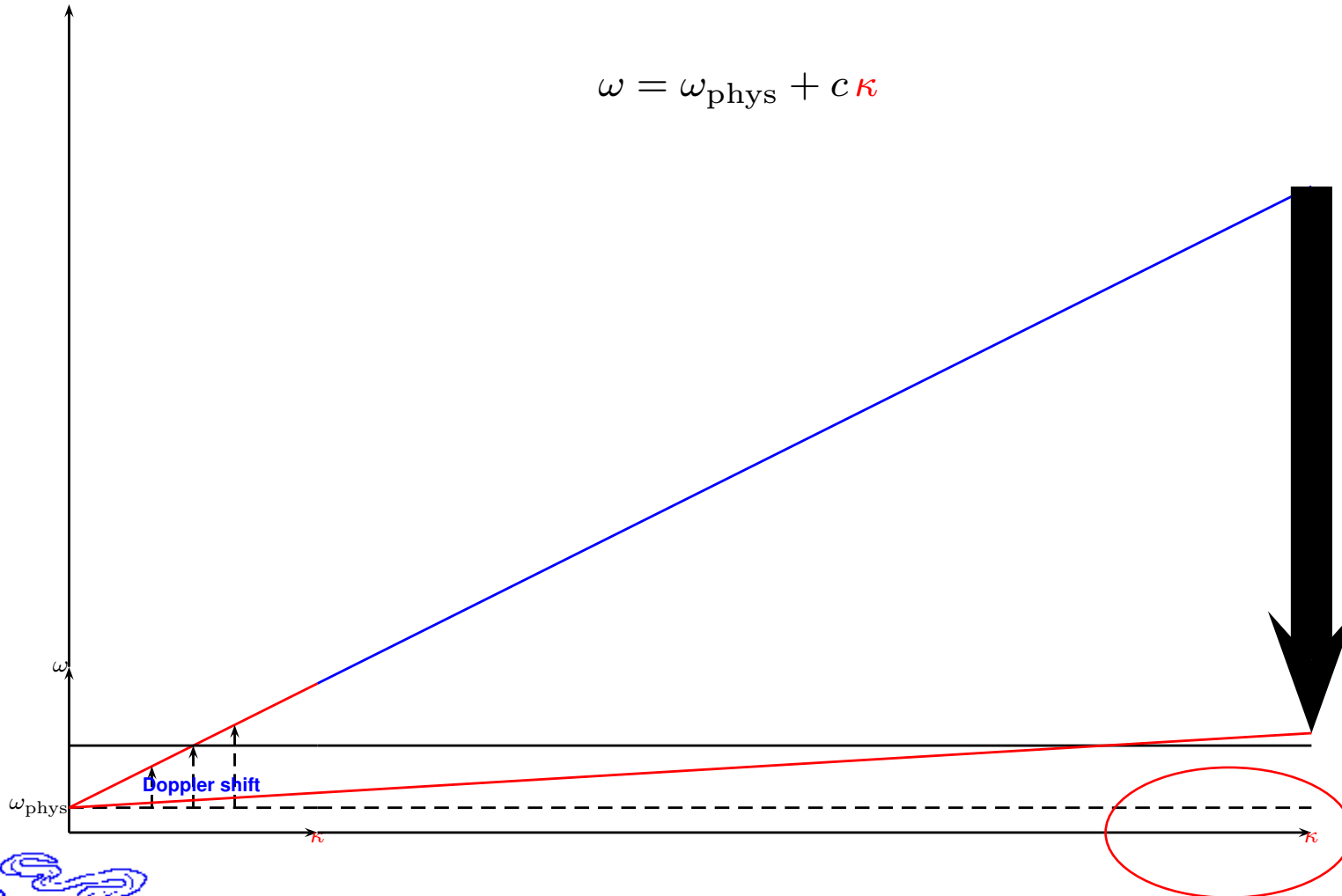


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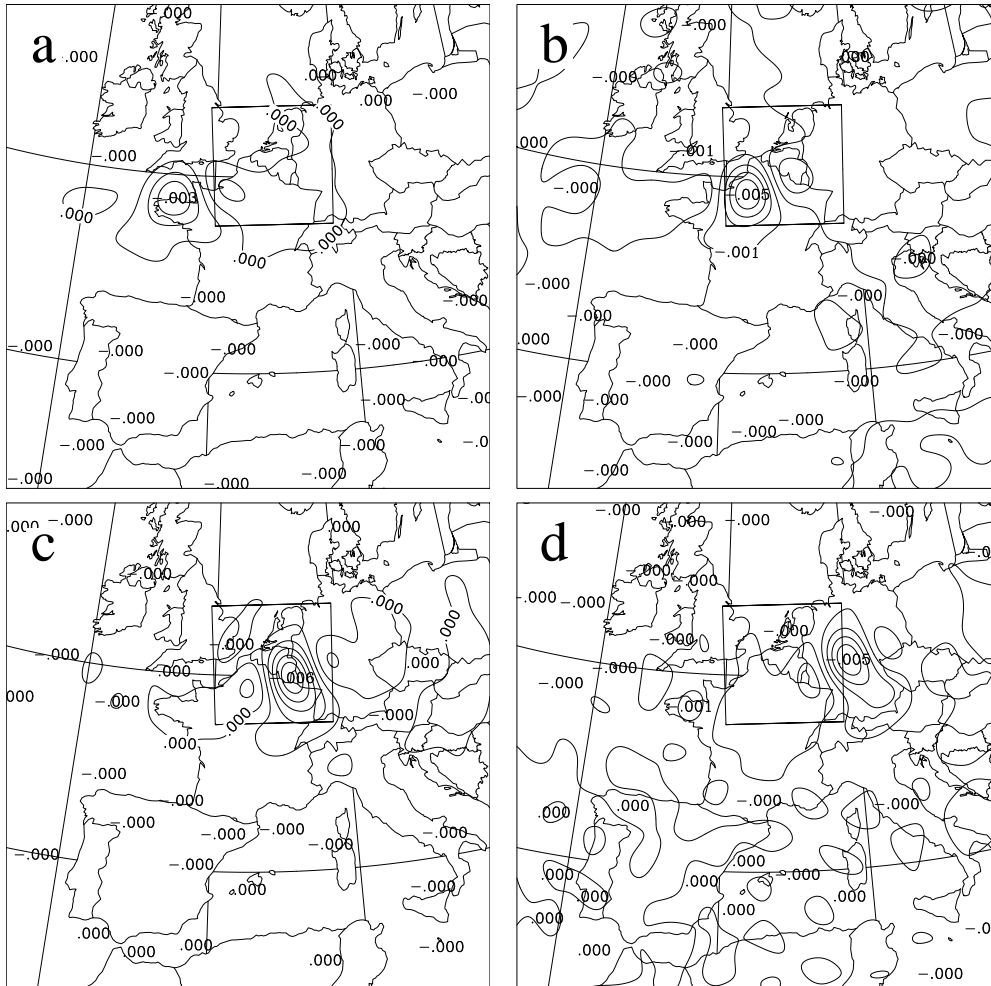
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MCUF + BER

Work of: P. Termonia, A Deckmyn and R. Hamdi (Be)



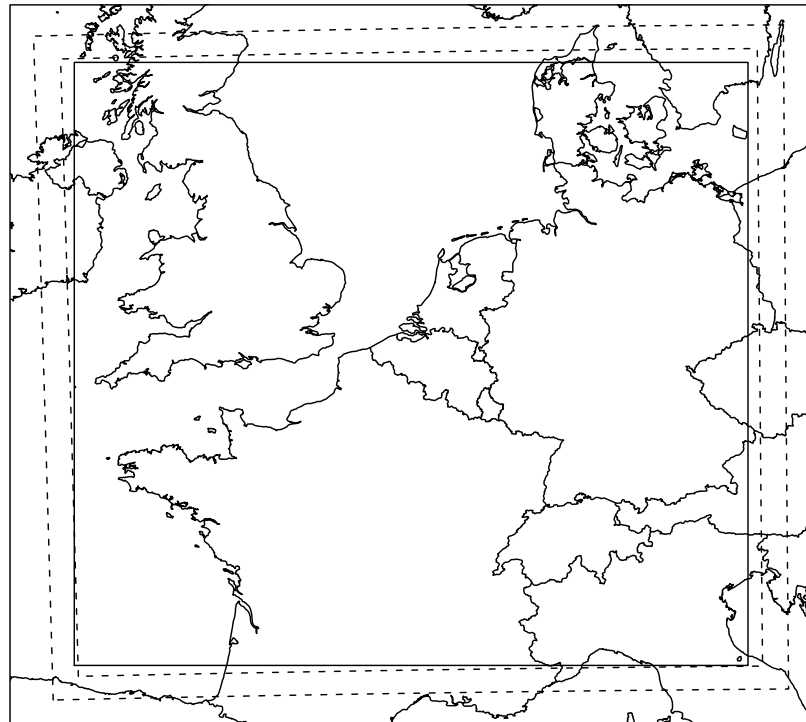
The monitoring by the MCUF field is done in ALADIN-France, i.e. the coupling model.



MCUF + BER



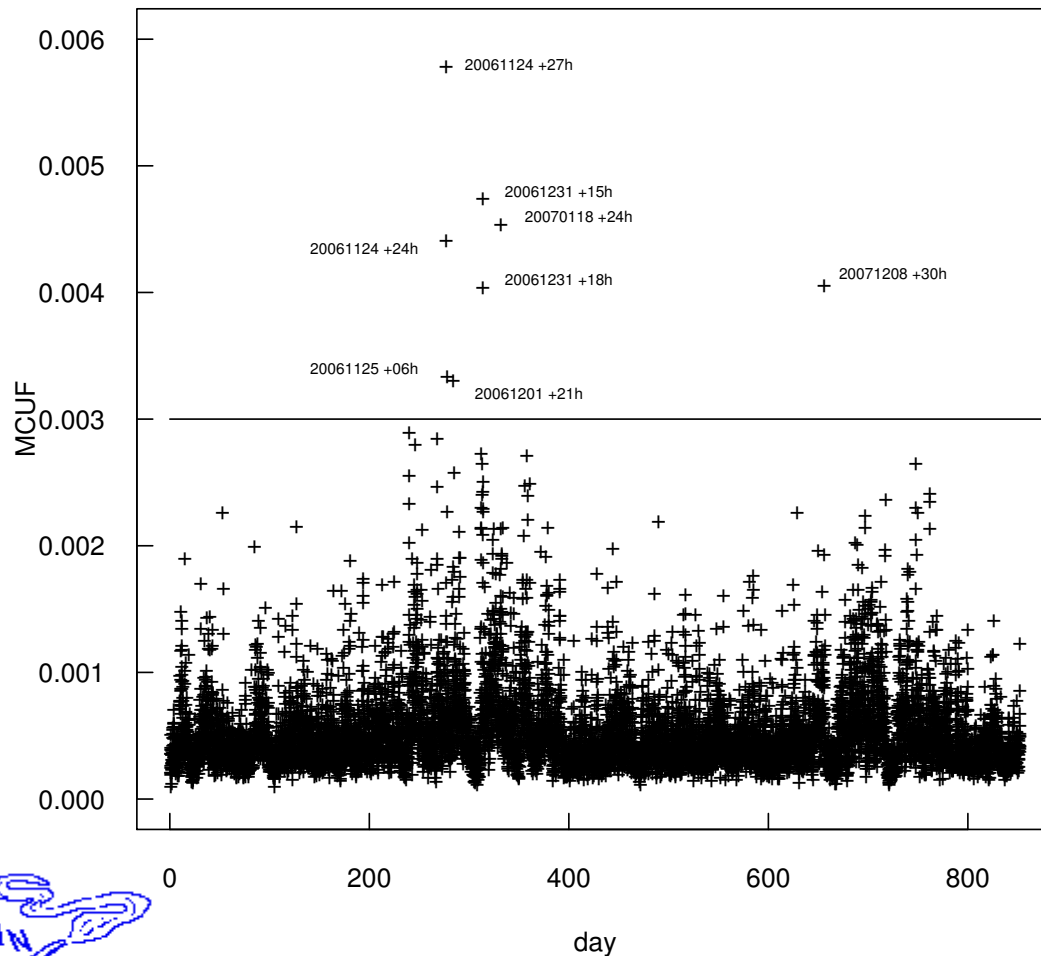
This MCUF field is operationally computed in ARPEGE and written to the coupling files of the ALADIN models. We considered it in the frame (solid line) covering the Davies zone (dashed),





MCUF + BER

The maximum MCUF in the frame
in the period 21 February 2006 – 30 June 2008



Let us consider
a threshold
value of 0.003.
Then we had 8
alerts.



MCUF + BER



The maximum MCUF in the frame

date	MCUF time	MCUF value	type	BER time
2006/11/24	+24h	0.0044	<i>incoming</i>	+27 h
	+27h	0.0058	<i>incoming</i>	+27 h
2006/11/25	+06h	0.0033	<i>incoming</i>	+09 h
2006/12/01	+21h	0.0033	corner (NE)	+24 h
2006/12/31	+15h	0.0047	tangent	+18 h
	+18h	0.0040	tangent	+18 h
2007/01/18	+24h	0.0045	outgoing	+ 30 h
2007/12/08	+30h	0.0041	<i>incoming</i>	+ 33 h

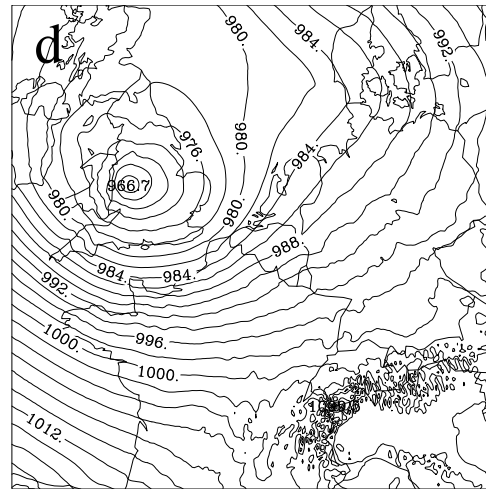
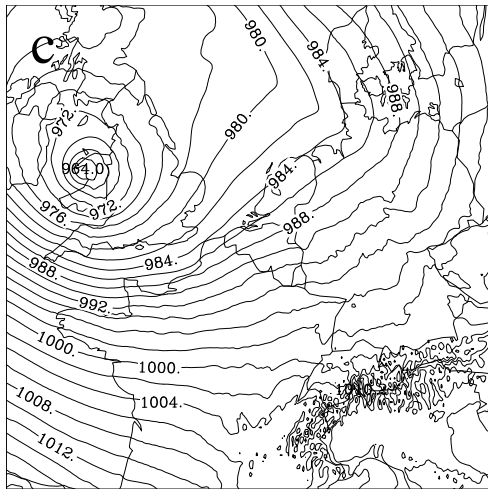
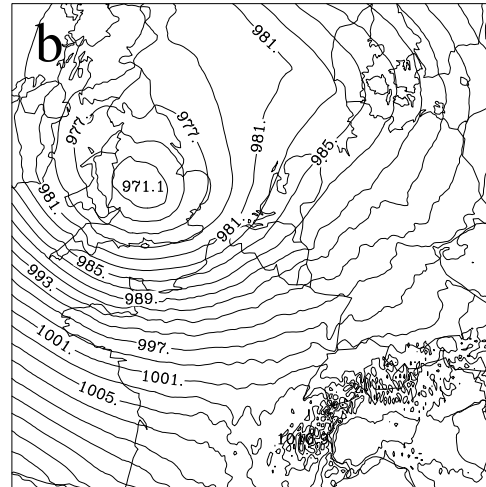
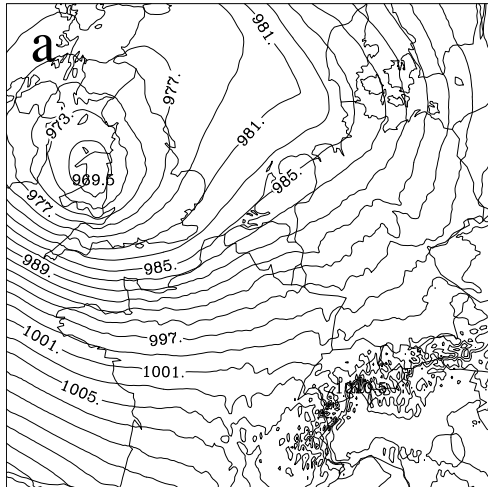
We carry out a restart 3 hours later than the MCUF alert: *Boundary-Error Restarts* (BER). However these restarts should be initialized by a SSDFI!!! Otherwise, we will filter out the low again in the restart in a way that is comparable to the loss at the boundary.





MCUF + BER

Improvements by a restart



(a) 33-h forecast range (969.5 hPa)

(b) 36-h forecast range (971.1 hPa)

(c) BER at 0900 UTC (964.0 hPa)

(d) BER at 1200 UTC (966.7 hPa).

⇒ 4.4 hPa improvement.

